

modes of the electronic ballast can be divided to intervals I, II, III, and IV.

Fig. 5 shows the block diagram of the control circuit for the proposed electronic ballast. The line-voltage sensing circuit is used to detect the line voltage for the MCU. When the sensed signal $v_z(t)$ from the line-voltage sensing circuit reaches zero level, the MCU begins to provide the low-frequency clock signals $V_{g,SL1}$ and $V_{g,SL2}$ with the twice line frequency for the low-frequency half-bridge driver. Furthermore, the MCU also provides the high-frequency clock signal V_{HF} to modulate the operating frequency of the PWM controller.

The current-sensing level-shifting technique [16-17] is employed to achieve the constant lamp power for the proposed electronic ballast. The duty ratio of the signal V_{PWM} can be controlled with the sensed signal $v_{cs}(t)$, which is the sum of the feedback signals $v_{lv}(t)$ and $v_{ic}(t)$. Then, the signal V_{PWM} from the PWM controller is fed into the high-frequency half-bridge driver to generate $V_{g,SH1}$ and $V_{g,SH2}$ by comparing with the signal $V_{g,SL2}$.

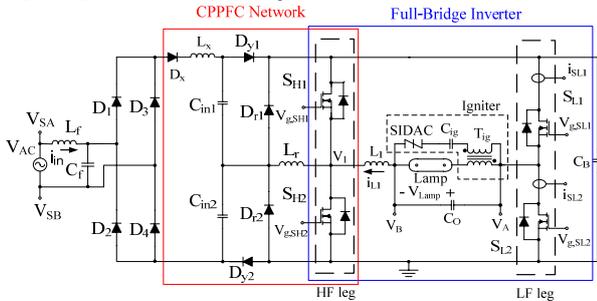


Fig. 3. Proposed single-stage CPPFC electronic ballast for MH Lamp.

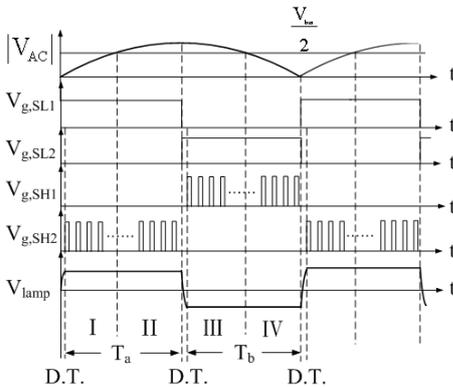


Fig. 4. Key waveforms of proposed electronic ballast.

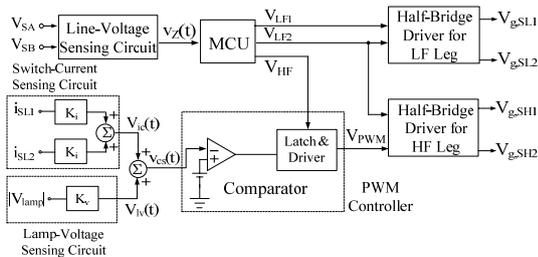


Fig. 5. Block diagram of control circuit for proposed electronic ballast.

III. OPERATIONAL PRINCIPLES

The operational principals of the electronic ballast in Interval-II are analyzed in this paper. The equivalent circuit and the key waveforms of the proposed electronic ballast in Interval-II are shown in Fig. 6 and Fig. 7, respectively. Fig. 8 shows the detailed key waveforms for the duration T_{a2} shown in Fig.7. Within one high-frequency switching cycle, the operational modes in Interval-II include eleven topological stages, as shown in Fig. 9. Referring to the Fig. 7, 8 and 9, the operational principles of the eleven topological stages in interval-II are described as follows.

Mode-1 [$t_0 \sim t_1$]: At $t=t_0$, the switch S_{H2} is turned on. The DC-bus voltage V_{bus} is applied to the C_0 - R_{lamp} - L_1 network. Therefore, the inductor current i_{L1} increases linearly. Meanwhile, the capacitor C_{in2} discharges to the resonant inductor L_r . When the capacitor voltage v_{Cin2} decreases to the rectified line voltage $|V_{AC}|$ at t_1 , the diode D_X conducts.

Mode-2 [$t_1 \sim t_2$]: The CP capacitor C_{in2} is discharged by the net current between the inductor currents i_{Lr} and i_X . When the voltage v_{Cin2} across the capacitor C_{in2} reaches zero at t_2 , the clamping diode D_{r2} conducts.

Mode-3 [$t_2 \sim t_3$]: The inductor L_X and the capacitor C_{in1} are charged by the line input current while the voltage level V_{Cin1} is lower than rectifier line voltage $|V_{AC}|$. The capacitor C_{in1} is charged by the inductor current i_X until the voltage v_{Cin1} reaches the DC bus voltage V_{bus} .

Mode-4 [$t_3 \sim t_4$]: The diodes D_{y1} and D_{y2} conduct at t_3 . The energy stored in the inductor L_X is released to the bulk capacitor C_B . Since the value of rectified line voltage $|V_{AC}|$ is lower than the DC bus voltage V_{bus} , the inductor current i_X decreases linearly.

Mode-5 [$t_4 \sim t_5$]: The body diode D_{SH1} of the switch S_{H1} conducts while the switch S_{H2} is turned off at t_4 . The energies stored in the inductors L_r and L_X transfer to the bulk capacitor C_B . In addition, the inductor L_1 discharges to the capacitor C_0 and the resistor R_{lamp} . When the inductor current i_X decreases to zero, this mode ends.

Mode-6 [$t_5 \sim t_6$]: The energy stored in inductors L_r is released to the bulk capacitor C_B until the inductor current i_{Lr} reaches zero.

Mode-7 [$t_6 \sim t_7$]: The diode D_{y1} conducts while the diode D_{r2} is turned off at t_6 . The capacitor C_{in1} discharges to the inductor L_r . The inductor current i_{Lr} decreases until the negative value of the inductor current i_{Lr} equals to the value of the inductor current i_{L1} .

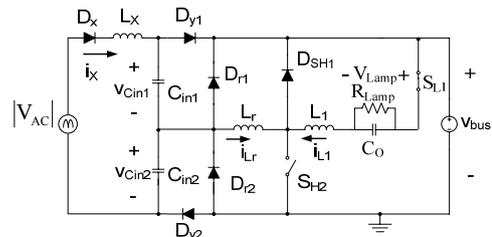


Fig. 6. Equivalent circuit of proposed electronic ballast in Interval-II.

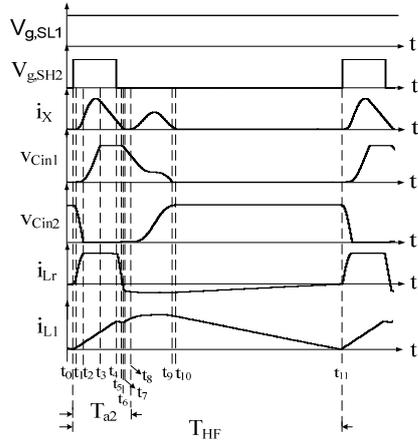


Fig. 7. Key waveforms of proposed electronic ballast in Interval-II.

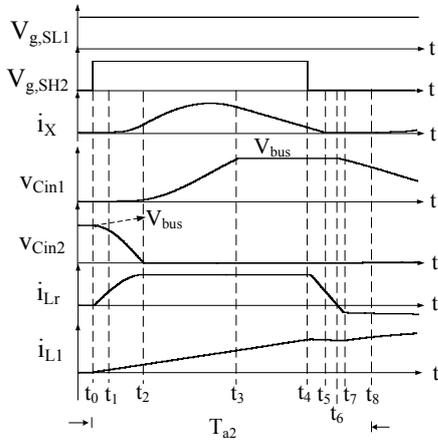


Fig. 8. Detailed key waveforms of Fig. 7 in duration T_{a2} .

Mode-8 [$t_7 \sim t_8$]: Since the voltage level of the capacitor C_{in1} is higher than the lamp voltage V_{lamp} , the CP capacitor C_{in1} discharges to the C_O - R_{lamp} - L_1 - L_r network. Therefore, the voltage V_{Cin1} decreases and the inductors currents i_{L1} and i_{Lr} increase. When the voltage V_{Cin1} reaches the rectified line voltage $|V_{AC}|$ at t_8 , the diode D_X conducts.

Mode-9 [$t_8 \sim t_9$]: The CP capacitor C_{in1} discharges to the C_O - R_{lamp} - L_1 - L_r network. Besides, the inductor L_X and capacitors C_{in1} , C_{in2} are charged by the line input current while the voltage level across the capacitors C_{in1} , C_{in2} is lower than rectifier line voltage $|V_{AC}|$. The capacitor C_{in1} is charged by the difference current between the inductor currents i_{L1} and i_X until the voltage v_{Cin1} reaches zero at t_9 .

Mode-10 [$t_9 \sim t_{10}$]: The inductors L_r and L_1 discharge to the resistor R_{lamp} and capacitor C_O . The inductor currents i_{L1} and i_{Lr} decreases linearly. The capacitor C_{in2} is charged by the inductor current i_X until the inductor current i_X reaches zero at t_{10} .

Mode-11 [$t_{10} \sim t_{11}$]: The inductors L_r and L_1 discharge to the capacitor C_O and resistor R_{lamp} . When the inductor currents i_{L1} and i_{Lr} reach zero at t_{11} , the switch S_{H2} is turned on and the next high-frequency switching cycle begins.

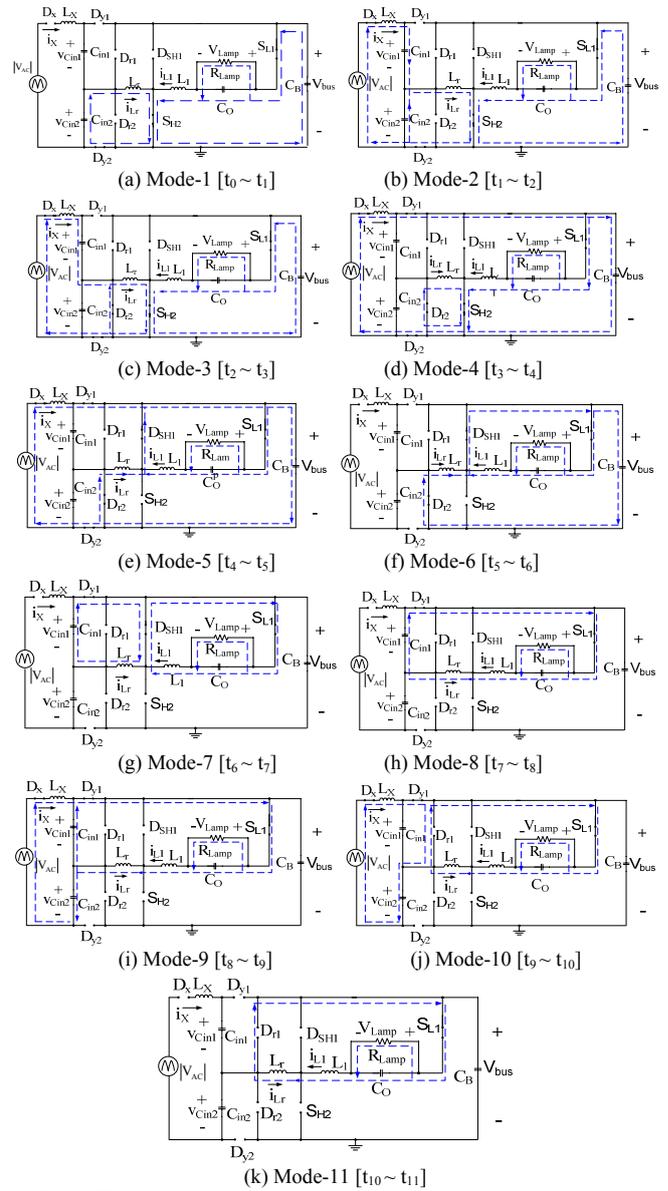


Fig. 9. Topological stages of proposed electronic ballast in Interval-II.

IV. DESIGN GUIDELINES

In order to simplify the derivation for the expression of the line current, the following assumptions are made:

- Steady-state operation and constant DC bus voltage,
- switches and diodes are ideal components,
- values of CP capacitors C_{in1} and C_{in2} are specified the same,
- resonant inductor L_r is neglected,
- i_{L1} during Mode-9 in Interval-II are assumed as a constant current source.

The equivalent circuits to represent the conducting paths of the inductor current i_X are shown in Fig. 10. And Fig. 11 shows the key waveforms of the equivalent circuits to represent the conducting paths of the inductor current i_X .

Mode-3 [$t_{a0} \sim t_{a1}$]

According to the equivalent circuit to represent the conducting path of the inductor current i_x during Mode-3 illustrated in Fig. 10(a), the inductor current $i_x(t)$ and the capacitor voltage $v_{Cin1}(t)$ can be obtained, as shown in Equations (1) and (2), respectively.

$$i_x(t) = \frac{|V_{AC}|}{Z_{X1}} \cdot \sin[\omega_{X1}(t - t_{a0})],$$

(1)

$$v_{Cin1}(t) = |V_{AC}| - |V_{AC}| \cos[\omega_{X1}(t - t_{a0})],$$

where

$$Z_{X1} = \sqrt{\frac{L_X}{C_{in1}}}, \text{ and}$$

$$\omega_{X1} = \frac{1}{\sqrt{L_X \cdot C_{in1}}}.$$

Mode-4 through Mode-5 [$t_{a1} \sim t_{a2}$]

According to the equivalent circuit to represent conducting path of the inductor current i_x during Mode-4 and Mode-5, as shown in Fig. 10(b), the inductor current $i_x(t)$ can be obtained, as shown in Equation (3).

$$i_x(t) = \frac{(|V_{AC}| - V_{bus})(t - t_{a1}) + \sqrt{2|V_{AC}| \cdot V_{bus} - V_{bus}^2}}{L_X Z_{X1}}. \quad (3)$$

Mode-9 [$t_{a3} \sim t_{a4}$]

According to the equivalent circuit to represent the conducting path of the inductor current i_x in Mode-9, as shown in Fig. 10(c), the inductor current $i_x(t)$ and the capacitor voltages $v_{Cin1}(t)$, $v_{Cin2}(t)$ can be obtained, as shown in Equations (4), (5), and (6), respectively.

$$i_x(t) = \frac{i_{L1}(t_{a3})}{2} - \frac{i_{L1}(t_{a3}) \cdot \cos[\sqrt{2}\omega_{X1}(t - t_{a3})]}{2}, \quad (4)$$

$$v_{Cin1}(t) = |V_{AC}| - \frac{i_{L1}(t_{a3}) \cdot (t - t_{a3})}{2 \cdot C_{in1}} - \frac{\sqrt{2} \cdot Z_{X1} \cdot i_{L1}(t_{a3}) \sin[\sqrt{2} \cdot \omega_{X1}(t - t_{a3})]}{4}, \quad (5)$$

$$v_{Cin2}(t) = \frac{i_{L1}(t_{a3}) \cdot (t - t_{a3})}{2C_{in1}} - \frac{\sqrt{2} \cdot i_{L1}(t_{a3}) \cdot Z_{X1} \cdot \sin[\sqrt{2} \cdot \omega_{X1}(t - t_{a3})]}{4}, \quad (6)$$

where $i_{L1}(t_{a3})$ is the initial value of the inductor current i_{L1} at t_{a3} .

Mode-10 [$t_{a4} \sim t_{a5}$]

According to the equivalent circuit to conducting path of the inductor current in Mode-10, as shown in Fig. 10(d), the inductor current $i_x(t)$ can be obtained, as shown in Equation (7).

$$i_x(t) = i_x(t_{a4}) \cdot \cos[\omega_{X1}(t - t_{a4})] + \frac{|V_{AC}|}{Z_{X1}} \cdot \sin[\omega_{X1}(t - t_{a4})] - \frac{v_{Cin2}(t_{a4})}{Z_{X1}} \sin[\omega_{X1}(t - t_{a4})], \quad (7)$$

where $i_x(t_{a4})$ and $v_{Cin2}(t_{a4})$ are the initial values of the inductor current i_x and the capacitor voltage v_{Cin2} at t_{a4} , respectively.

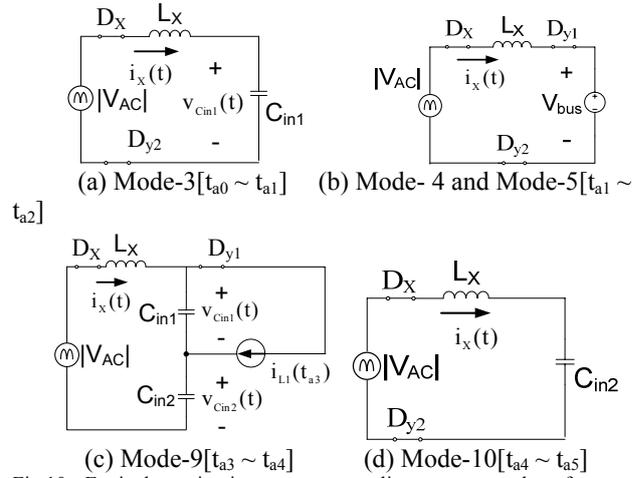


Fig.10. Equivalent circuits to represent line current paths of proposed electronic ballast in Interval-II.

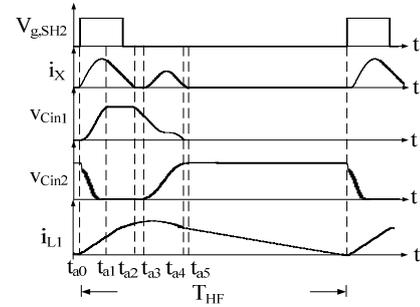


Fig. 11. Key waveforms for equivalent circuits to represent conducting paths of inductor current i_x

According to the preceding analysis, the average line current i_{in_avg} over one high-frequency switching cycle in Interval-II can be obtained as shown in Equation (8).

$$i_{in_avg} = i_{x_avg} = \frac{1}{T_{HF}} \left[\int_{t_{a0}}^{t_{a2}} i_x(t) dt + \int_{t_{a3}}^{t_{a5}} i_x(t) dt \right]. \quad (8)$$

By substituting Equations (1), (3), (4), and (7) into Equation (8), the average line current equation in Interval-II can be rewritten, as shown in Equation (9).

$$i_{in_avg} = \frac{1}{T_{HF}} \left[K_1 \cdot |V_{AC}| + K_2 + K_3 + K_4 \right], \quad (9)$$

where $K_1 = C_{in1} \cdot (2 - \cos(\omega_{X1} \cdot T_{A_1}) - \cos(\omega_{X1} \cdot (T_{A_4})))$,

$$K_2 = \frac{C_{in1} \cdot V_{bus} \cdot (2 \cdot |V_{AC}| - V_{bus})}{2(V_{bus} - V_{AC})},$$

$$K_3 = \frac{i_{L1}(t_{a3}) \cdot T_{A_3} \cdot \sin(\sqrt{2}\omega_{X1} \cdot T_{A_3})}{2 \cdot 2 \cdot \omega_{X1}},$$

$$K_4 = \frac{i_x(t_{a4}) \cdot \sin(\omega_{X1} \cdot T_{A_4})}{\omega_{X1}} + v_{Cin2}(t_{a4}) \cdot C_{in1} (1 - \cos(\omega_{X1} T_{A_4})),$$

$$T_{A_1} = t_{a1} - t_{a0},$$

$$T_{A_3} = t_{a4} - t_{a3}, \text{ and}$$

$$T_{A_4} = t_{a5} - t_{a4}$$

Based on the energy conservation between the input power and output power, Equation (10) can be obtained as follows:

$$\frac{P_o}{\eta} = V_{AC_rms} \cdot I_{in_rms} = \frac{V_{AC_pk} \cdot I_{in_pk}}{2} \quad (10)$$

where

P_o is the lamp power,

η is the conversion efficiency,

V_{ac_pk} is the peak value of the line voltage, and

I_{in_pk} is the peak value of the line current.

Based on Equation (9) and Equation (10), the expression of the CP capacitor C_{in1} can be derived, as shown in Equation (11).

$$C_{in1} = (1.23 \cdot 10^{-4} \cdot K_a + 111K_a \sqrt{(1.23 \cdot 10^{-4} \cdot K_a + 6.57 \cdot 10^{-4} \cdot K_b + 4 \cdot 10^{-4} \cdot K_c)} + 3.28 \cdot 10^{-4} \cdot K_b - 2 \cdot 10^{-4} \cdot K_c) \times \frac{50(V_{AC_pk} - V_{bus})}{[K_d - 500V_{bus}^2]^2 V_{AC_pk} \cdot \eta} \quad (11)$$

where

$$K_a = V_{AC_pk} \cdot \eta \cdot L_x \cdot i_{L1}(t_{a1})^2 (V_{AC_pk} - V_{bus}),$$

$$K_b = T_{HF} \cdot P_o \cdot L_x \cdot i_{L1}(t_{a1}) (V_{AC_pk} - V_{bus}),$$

$$K_c = T_{HF} \cdot P_o \cdot V_{bus}^2, \text{ and}$$

$$K_d = 821 \cdot L_x \cdot i_{L1}(t_{a1}) (V_{AC_pk} - V_{bus}).$$

At $t = \frac{\pi}{2 \cdot \omega_{x1}} + t_{a0}$, Equation (1) can be rewritten as Equation

(12) in order to calculate the inductor peak current i_{X_pk} .

$$i_{X_pk} = \sqrt{\frac{C_{in1}}{L_x} \cdot V_{AC_pk}} \quad (12)$$

Combining Equations (11) and (12), the expression of the inductance L_x can be derived, as shown in Equation (13).

$$L_x = \frac{\eta^2 \cdot C_{in1} \cdot V_{AC_pk}^4}{4 \cdot P_o^2 \cdot K_e^2} \quad (13)$$

where

$$K_e = \frac{i_{X_pk}}{i_{in_pk}}$$

The specifications for the proposed electronic ballast are listed in Table 1. Plotted from Equation (11), Fig. 12 shows the relationship between the values of the CP capacitors C_{in1} , C_{in2} and the DC-bus voltage V_{bus} with different values of inductor L_x . Fig. 12 shows that the DC-bus voltage V_{bus} increases as the values of the CP capacitors C_{in1} and C_{in2} increase.

Plotted from Equation (13), Fig. 13 shows the relationship between the value of inductor L_x versus the value of CP capacitors C_{in1} and C_{in2} with different value for factor K_e . According to Fig. 13, the value of inductor L_x increases as the values of the CP capacitors C_{in1} and C_{in2} increase.

By applying $\eta=0.8$, $V_{bus}=380V$, $K_e=5$, $i_{L1}(t_{c3})=0.796$ A, and the specifications in Table 1 to Equations (11) and (13), the value of the CP capacitors C_{in1} , C_{in2} and the value of the inductor L_x can be calculated as 4.37nF and 312 μ H, respectively.

Table 1. Specifications of prototype circuit.

Specifications	Values
Input AC Voltage V_{AC}	200 V_{rms} to 242 V_{rms} , at 60Hz
Rated Lamp Voltage V_{Lamp}	88 V_{rms}
Rated Lamp Current I_{Lamp}	398mA
Rated Lamp Power P_{Lamp}	35W
Operating Frequency of LF Leg f_{LF}	120 Hz
Switching Frequency of HF Leg f_{HF}	50 kHz

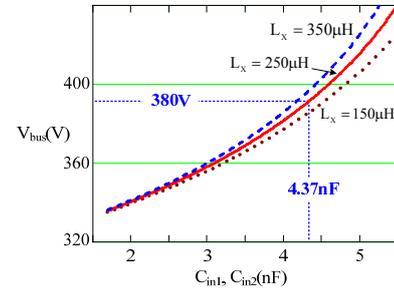


Fig. 12. Relationship between value of the CP capacitors C_{in1} , C_{in2} and DC-bus voltage.

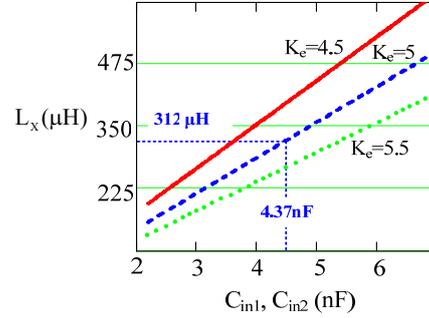


Fig. 13. Relationship between value of inductor L_x versus value of CP capacitors C_{in1} and C_{in2} with different factor K_e .

V. EXPERIMENTAL RESULTS

Based on the specifications and the parameters, listed in Tables 1 and 2, respectively, a prototype circuit for 35W MH lamp is implemented to validate the presented design criteria.

Fig. 14 shows the measured waveforms of the input voltage and the input current at 220 V_{rms} input voltage. Fig. 15 illustrates the comparison between the measured input current harmonic and the IEC 61000-3-2 Class-C Standard. The measured PF and THD are 0.976 and 16.3%, respectively.

In Fig. 16, the lamp voltage and current waveforms at steady-state are 88.7 V_{rms} and 409 mA, respectively. Fig. 17 shows the photo of the shaking-free arc in the MH lamp. The

